

Main Ideas/Questions	Notes
PROPERTIES OF Parallelograms	① opposite sides are \cong (congruent)
	② opposite sides are parallel
	③ opposite angles are \cong
	④ consecutive angles are supplementary (sum 180)
	⑤ diagonals bisect each other - segments are cut in half.

Directions: Each quadrilateral below is a parallelogram. Find the missing measures.

1.

$AD = 8$
 $DC = 15$
 $m\angle A = 68^\circ$
 $m\angle B = 112^\circ$
 $m\angle C = 112^\circ$

2.

$JK = 21$
 $KL = 29$
 $m\angle J = 127^\circ$
 $m\angle K = 53^\circ$
 $m\angle M = 53^\circ$

3.

$UV = 7$
 $ST = 18$
 $VS = 7$
 $VT = 15$
 $*RT = 30$

4.

$m\angle DEC = 63^\circ$
 $m\angle CDE = 46^\circ$
 $m\angle ECD = 71^\circ$
 $m\angle DFE = 25^\circ$
 $*m\angle FED = 134^\circ$
 $21 + y + 71 + 63 = 180$
 $y = 25$

formula given
Distance
Formula
*do not have to memorize

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

EXAMPLE:
Find the length of segment AB given A (-4, 1) and B (3, -1).
 $\sqrt{(-4-3)^2 + (1-(-1))^2}$
 $\sqrt{7^2 + (-2)^2}$
 $\sqrt{49+4}$
 $\sqrt{53}$

Slope Formula
*formula not given to you

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{rise}}{\text{run}}$$

EXAMPLE:
Find the slope of segment AB given A (-4, 1) and B (3, -1).
 $m = \frac{-1-1}{3-(-4)} = \frac{-2}{7}$

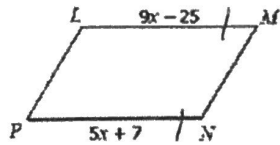
Slopes of Parallel Lines

The slopes of parallel lines are the same.

EXAMPLE:
Are there the opposite side of this quadrilateral parallel?
 $m_{AD} = \frac{-4}{1} = -4$
 $m_{BC} = \frac{-4}{1} = -4$
 $m_{AB} = \frac{0}{7} = 0$
 $m_{DC} = \frac{0}{7} = 0$

yes

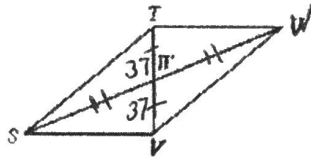
7. Solve for x.



$$\begin{aligned} 9x - 25 &= 5x + 7 \\ -5x & \quad -5x \\ 4x - 25 &= 7 \\ 4x &= 32 \end{aligned}$$

$$\boxed{x = 8}$$

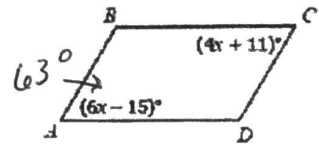
9. If $TV = 74$ and $WV = 4x + 1$, solve for x.



$$\begin{aligned} 4x + 1 &= 37 \\ 4x &= 36 \end{aligned}$$

$$\boxed{x = 9}$$

11. Find $m\angle B$.

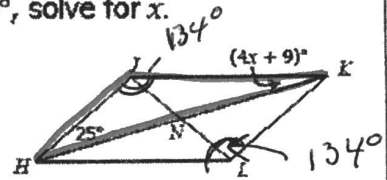


$$6x - 15 = 4x + 11 \quad 6(13) - 15 = 63$$

$$\boxed{x = 13}$$

$$\boxed{m\angle B = 63^\circ}$$

13. If $m\angle KLH = 134^\circ$, solve for x.



$$\begin{aligned} 25 + 134 + 4x + 9 &= 180 \\ 4x + 168 &= 180 \\ 4x &= 12 \end{aligned}$$

$$\boxed{x = 3}$$

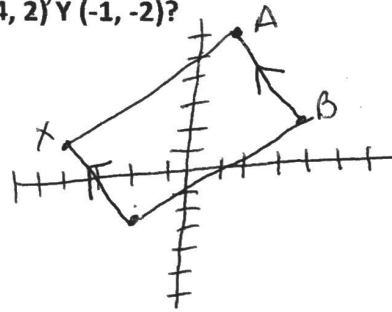
Is segment AB parallel to segment XY given that A (1, 6) B (4, 2) X (-4, 2) Y (-1, -2)?

check slopes

$$m = \frac{2-6}{4-1} = \frac{-4}{3}$$

$$m = \frac{-2-2}{-1-4} = \frac{-4}{3}$$

yes
because their
slopes are the
same



Find the length of each side of quadrilateral ABCD given that A (1, 6) B (4, 2) X (-4, 2) Y (-1, -2)?

distance formula $X(-4, 2)$ $A(1, 6)$

$$d_{AX} = \sqrt{(1+4)^2 + (6-2)^2}$$

$$= \sqrt{5+4^2}$$

$$= \sqrt{25+16}$$

$$= \sqrt{41}$$

$B(4, 2)$ $Y(-1, -2)$

$$d_{BY} = \sqrt{(-1-4)^2 + (-2-2)^2}$$

$$= \sqrt{(-5)^2 + (-4)^2}$$

$$= \sqrt{25+16}$$

$$= \sqrt{41}$$