

# Pythagorean Theorem Review

- What types of triangles can we use the Pythagorean theorem for?  
 (-right, acute, obtuse, isosceles, scalene, equilateral?)

↳ Can also use to det. if a  $\Delta$ 's acute or obtuse.

- What do we use the Pythagorean Theorem for?

When we have 2 sidelengths & are looking for 3rd.

- What is the formula?

$$a^2 + b^2 = c^2$$

- What is a Pythagorean Triple?

All 3 sides of a right triangle are whole #'s.

Practice:



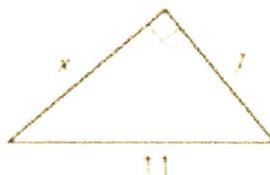
$$3^2 + 9^2 = x^2$$

$$9 + 81 = x^2$$

$$90 = x^2$$

$$\sqrt{90} = x$$

$$\begin{matrix} & \wedge & \\ 10 & 9 & \\ \wedge & \wedge & \\ 5 & 3 & \end{matrix} \quad \boxed{3\sqrt{10} = x}$$



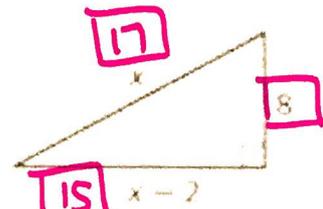
$$x^2 + 7^2 = 11^2$$

$$x^2 + 49 = 121$$

$$x^2 = 72$$

$$x = \sqrt{72}$$

$$\begin{matrix} & \wedge & \\ 8 & 9 & \\ \wedge & \wedge & \\ 4 & 2 & \end{matrix} \quad \begin{matrix} \wedge & \wedge \\ 2 & 3 \end{matrix} \quad \boxed{x = 6\sqrt{2}}$$



$$(x-2)^2 + 8^2 = x^2$$

$$(x-2)(x-2) + 64 = x^2$$

$$x^2 - 2x - 2x + 4 + 64 = x^2$$

$$x^2 - 4x + 68 = x^2$$

$$\begin{array}{r} -x^2 \qquad \qquad -x^2 \\ \hline -4x + 68 = 0 \\ +4x \qquad \qquad +4x \\ \hline 68 = 4x \end{array}$$

$$x = 17$$

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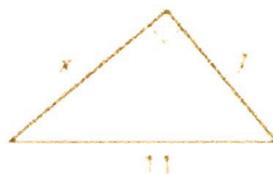
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$$\begin{array}{c} \wedge \\ 10 \quad 9 \\ \wedge \quad \wedge \\ 5 \quad 2 \quad (55) \end{array} \quad \boxed{3\sqrt{10} = x}$$



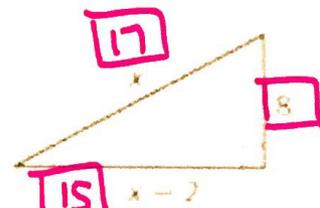
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$$x^2 + 49 = 121$$

$$x^2 = 72$$

$$x = \sqrt{72}$$

$$\begin{array}{c} \wedge \\ 8 \quad 9 \\ \wedge \quad \wedge \\ 4 \quad 2 \quad (33) \\ \wedge \\ (22) \end{array} \quad \boxed{x = 6\sqrt{2}}$$



$$(x-2)^2 + 8^2 = x^2$$

$$(x-2)(x-2) + 64 = x^2$$

$$x^2 - 2x - 2x + 4 + 64 = x^2$$

$$x^2 - 4x + 68 = x^2$$

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$$68 = 4x$$

$$\boxed{x = 17}$$

# Converse of the Pythagorean Theorem

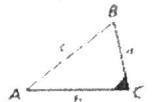
# Pythagorean Inequalities Theorem

**Theorems 9-1-1 Converse of the Pythagorean Theorem**

THEOREM	HYPOTHESIS	CONCLUSION
If the sum of the squares of the lengths of two sides of a triangle is equal to the square of the length of the third side, then the triangle is a right triangle.	 $a^2 + b^2 = c^2$	$\triangle ABC$ is a right triangle.

**Theorems 9-1-2 Pythagorean Inequalities Theorem**

In  $\triangle ABC$ ,  $c$  is the length of the longest side.

If $c^2 > a^2 + b^2$ , then $\triangle ABC$ is an obtuse triangle.		If $c^2 < a^2 + b^2$ , then $\triangle ABC$ is an acute triangle.	
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Ex: Do these 3 sides make a right triangle?

1. 9, 40, 41

$$9^2 + 40^2 \stackrel{?}{=} 41^2$$

$$81 + 1600 \stackrel{?}{=} 1681$$

$$1681 \stackrel{?}{=} 1681$$

yes, its a rt  $\Delta$ .

Ex: Are these acute or obtuse triangles?

1. 9, 11, 15

2. 7, 10, 12

$$1) 15^2 \stackrel{?}{=} 9^2 + 11^2$$

$$225 \stackrel{?}{=} 81 + 121$$

$$225 \stackrel{?}{=} 202$$

obtuse  $\Delta$

(hyp is greater)

$$2) 12^2 \stackrel{?}{=} 7^2 + 10^2$$

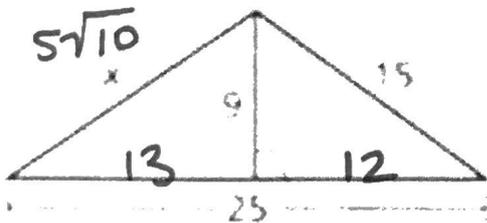
$$144 \stackrel{?}{=} 49 + 100$$

$$144 \stackrel{?}{=} 149$$

Acute  $\Delta$

(hyp is less than legs)

Simplest Radical form Review: than legs)



$$9^2 + x^2 = 15^2$$

$$81 + x^2 = 225$$

$$\begin{array}{r} -81 \\ \hline \end{array}$$

$$x^2 = 144$$

$$x = 12$$

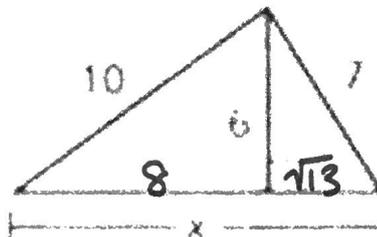
$$9^2 + 13^2 = x^2$$

$$81 + 169 = x^2$$

$$250 = x^2$$

$$\sqrt{250} = x$$

$$x = 5\sqrt{10}$$



$$6^2 + x^2 = 10^2$$

$$36 + x^2 = 100$$

$$x^2 = 64$$

$$x = 8$$

$$6^2 + x^2 = 7^2$$

$$36 + x^2 = 49$$

$$x^2 = 13$$

$$x = \sqrt{13}$$

$8 + \sqrt{13}$